## 10.1/11.3 Circumference \& Arc Length and Area of Circles \& Sectors


center

## Goals Aligned to Common Core State Standards:

- You will identify the center, chord, diameter, and radius of a circle.
- You will understand all circles as similar and derive the formula for the area of a sector.
- You will solve problems involving the radii, diameters, circumference, arc length and areas of circles and sectors.
- MP 1, 2, 6, 7, 8

A circle is a set of points whose distance around a fixed point is constant.

Radius Formula $r=\frac{d}{2}$ or $r=\frac{1}{2} d$
Diameter Formula $d=2 r$

Two circles are congruent circles if and only if they have congruent radii.

Concentric circles are coplanar circles that have the same center.


$$
\begin{gathered}
C=\pi d \text { or } C=2 \pi r \\
A=\pi r^{2}
\end{gathered}
$$

EX. 2 Find the circumference, diameter, or radius.
a.) Find C if $\mathrm{r}=7 \mathrm{~cm}$
b.) Find C if $\mathrm{d}=12.5$ in

$$
2 \pi 7=43.98 \mathrm{~cm} \quad \begin{aligned}
C & =\pi(12.5) \\
& C=39.27
\end{aligned}
$$

c.) $C=136.9$ find $D$
d.) Find $r$
e.) Find the area

$$
\begin{array}{ll}
\frac{136.9}{\pi}=\frac{\pi D}{\pi} \\
43.58 & =D
\end{array}
$$

$$
\begin{aligned}
& \pi(21.79)^{2} \\
& 1493.41 \mathrm{un}
\end{aligned}
$$

Find the exact circumference of $\odot K$.


Find the exact area.

$$
9 \pi \pi\left(3^{2}\right)=9 \pi
$$

MANUFACTURING An outdoor accessories company manufactures circular covers for outdoor umbrellas. If the cover is 8 inches longer than the umbrella on each side, find the area of the cover in square inches.

$44^{2} \pi$<br>$1936 \pi$



ALGEBRA Find the radius of a circle with an area of 58 square inches.

$$
r=4.3 \begin{aligned}
\frac{58}{\pi} & =\frac{\pi r^{2}}{\pi} \\
\sqrt{\frac{58}{\pi}} & =\sqrt{r^{2}} \\
4.3 & =r
\end{aligned}
$$



PIE A pie has a diameter of 9 inches and is cut into 10 congruent slices. What is the area of one slice to the nearest hundredth?

$$
\begin{aligned}
& \text { slice to the nearest hundredth? } \\
& A=\frac{x}{360} \cdot \pi r^{2} \\
& \frac{360}{10}=36 \quad \frac{36}{360} \cdot \pi(9)^{2}=25.45 \mathrm{in}^{2}
\end{aligned}
$$

Arc Length Formula:

$$
l=\frac{x}{360} \cdot 2 \pi r
$$


A. Find the length of $\overparen{D A}$. Round to the nearest hundredth.

$$
\begin{aligned}
& l=\frac{40}{360} \cdot 2 \cdot \pi \cdot 4.5 \\
& l=3.14 \mathrm{~cm}
\end{aligned}
$$



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