### 5.5 Triangle Inequality

## Goals aligned to the Common Core State Standards:

- You will use the Triangle Inequality Theorem to identify possible triangles and to prove triangle relationships.

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## Theorem 5.11

Triangle Inequality Theorem
The sum of the lengths of any two sides of a triangle must be greater than the length of the third side.

$$
\text { Examples } \begin{aligned}
P Q+Q R>P R \\
Q R+P R>P Q \\
P R+P Q>Q R
\end{aligned}
$$



Ex. 1 Determine whether the given measures can be the lengths of the sides of a triangle. Write yes or no, explain.
a.) $5,4,3$

$$
\begin{aligned}
3+4 & >5 \\
7 & >5
\end{aligned}
$$


b.) $5,15,10$

$$
5+10>15
$$

c.) $30.1,0.8,31$

$$
\begin{aligned}
& 10>15 \\
& 15>15 \text { no }
\end{aligned}
$$

$$
\begin{array}{r}
30.1+0.8>31 \\
30.9 \ngtr 31
\end{array}
$$

d.) $5.6,10.1,5.2$

$$
5.6+5.2>10.1 \text { yes }
$$

Ex. 2 Find the range for the measure of the $3^{\text {rd }}$ side of a triangle given the measures of the two sides.
a.) 7 and 12

$$
\begin{aligned}
& 12-7=5 \\
& 12+7=19
\end{aligned}
$$

b.) 14 and 23

$$
\begin{aligned}
& 23-14=9 \\
& 23+14=37
\end{aligned}
$$



$$
9<x<37
$$

Homework:
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