

Chapter 3.4 Equations of Lines Notes

- Goals:
- You will write equations for parallel and perpendicular lines.

Slope – intercept form

- Equation: $y = mx + b$
- Variables: $m \rightarrow$ slope $b \rightarrow$ y-intercept

Point – slope form

- Equation: $y - y_1 = m(x - x_1)$
- Variables: $m \rightarrow$ slope $(x_1, y_1) \rightarrow$ point

Example 1 Write an equation in slope-intercept form of the line with slope -2 and y-intercept 4 .

$$y = -2x + 4$$

Example 2 Write an equation in point-slope form of the line with slope $-\frac{3}{4}$ that contains $(8, 1)$.

$$y - 1 = -\frac{3}{4}(x - 8)$$

Example 3: Change your answer from example 2 to slope-intercept form.

$$\begin{aligned} y - 1 &= -\frac{3}{4}x + 6 \\ +1 & \quad +1 \\ \hline y &= -\frac{3}{4}x + 7 \end{aligned}$$

Example 4: What if the question asked to write an equation in point-slope form of the line with a parallel slope? Perpendicular?

Same \rightarrow

$$\text{slope} \rightarrow \frac{4}{3}$$

Example 5: Write an equation in slope-intercept form for a line that goes through points $(4, 9)$ and $(-2, 0)$.

$$\frac{9 - 0}{4 - (-2)} = \frac{9}{6} = \frac{3}{2} = m$$

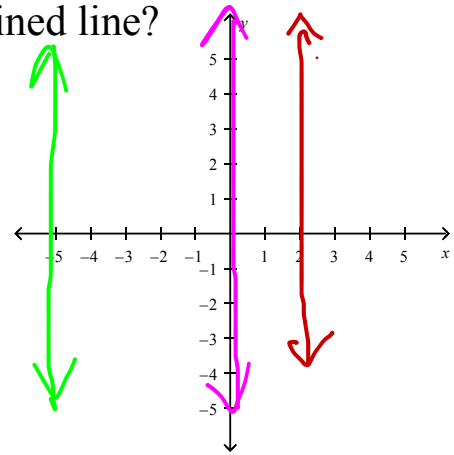
$$\begin{aligned} y - 0 &= \frac{3}{2}(x - (-2)) \\ \boxed{y} &= \frac{3}{2}x + 3 \end{aligned}$$

How do you write the equation of an undefined line?

$$x=2$$

$$x=0$$

$$x=-5$$



Extra questions:

Write the following equations in slope-intercept form:

1. A line that passes through the point $(4, -3)$ with a slope of -2 .

$$y - (-3) = -2(x - 4)$$

$$y + 3 = -2x + 8$$

$$y = -2x + 5$$

2. A line that is parallel to a line with a slope of $\frac{2}{3}$ and passes through the point $(6, -1)$.

$$y - (-1) = \frac{2}{3}(x - 6)$$

$$y + 1 = \frac{2}{3}x - 4$$

$$y = \frac{2}{3}x - 5$$

3. A line that is perpendicular to a line with a slope of $\frac{2}{3}$ and passes through the point $(6, -1)$.

$$\perp -\frac{3}{2}$$

$$y - (-1) = -\frac{3}{2}(x - 6)$$

$$y + 1 = -\frac{3}{2}x + 9$$

$$y = -\frac{3}{2}x + 8$$

4. A line that contains the two points $(1, 6)$ and $(3, 2)$.

$$\frac{6-2}{1-3} = \frac{4}{-2} = -2$$

$$y - 6 = -2(x - 1)$$

$$y - 6 = -2x + 2$$

$$y = -2x + 8$$

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 - *You will write equations for parallel and perpendicular lines.*
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Writing Equations Wkst including task